

Robust Channel Estimation for OFDM Wireless Communication Systems—An H_∞ Approach

Jun Cai, *Student Member, IEEE*, Xuemin Shen, *Senior Member, IEEE*, and Jon W. Mark, *Life Fellow, IEEE*

Abstract—In this paper, the joint time–frequency domain channel estimation problem in orthogonal frequency-division multiplexing (OFDM) wireless communication systems is transformed to a set of independent time-domain estimation problems. A robust channel estimation algorithm based on the H_∞ filtering approach is proposed to estimate the channel fading in the time domain. The estimation criterion is to minimize the worst possible amplification of the estimation errors in terms of the exogenous input disturbances such as multiplicative and additive noise. The criterion is different from the traditional minimum estimation error variance criterion for the Kalman estimation algorithm, and requires no *a priori* knowledge of the disturbance statistics. It is shown that the proposed channel estimation algorithm is more robust compared with the Kalman estimation counterpart in terms of model uncertainty, and is more suitable to practical OFDM wireless communication systems.

Index Terms—Channel estimation, orthogonal frequency-division multiplexing (OFDM), H_∞ filtering, wireless communications.

I. INTRODUCTION

THE high demand for a large volume of multimedia services in wireless communication systems requires high transmission rates. However, high transmission rates may result in severer frequency selective fading and intersymbol interference (ISI) if the bandwidth of the transmitted signal is large compared to the coherence bandwidth of the channel. Orthogonal frequency-division multiplexing (OFDM) has been proposed to combat these types of channel disturbance [1]–[4]. In an OFDM system, the signal is transformed into a number of components, each with a bandwidth narrower than the coherence bandwidth of the propagation channel. Each of the OFDM signal components is modulated onto a distinct subcarrier. With OFDM, the transmission in each subcarrier experiences frequency flat fading, and OFDM is said to have transformed frequency-selective fading to flat fading.

Channel state information is very important to achieve optimal diversity combining and coherent detection at the receiving end. In the absence of channel state information, channel estimators can be used to provide estimates of the channel state information. In OFDM, channel fading information is present in both the time and frequency domains. A proper

channel estimation algorithm for the OFDM systems should capture both the time- and frequency-domain characteristics. In recent years, channel estimation for OFDM systems has been a very active research area, both in the time domain [6]–[9] and in the frequency domain [4], [10], [11]. By representing the correlation function of the channel fading as the product of the correlation functions in the time domain and the frequency domain, it is possible to perform channel estimation in the time domain alone [5]. To our knowledge, the development of estimation algorithms has been based on known statistics of the fading channel and the additive noise. The criterion used is minimization of the variance of the estimation errors, e.g., the Kalman estimation algorithm. On the basis of known channel statistics, the Kalman estimator is optimal in the sense that the error covariance is minimized. However, in practical systems, channel statistics are not completely known. When the Kalman estimator is not the dual of the channel, the performance of the Kalman estimator may suffer significant degradation [12]. A robust channel estimator for practical OFDM wireless communication systems, which does not depend on *a priori* knowledge of the channel state information, is desirable. This is the motivation behind the work presented in this paper.

In this paper, the two-dimensional time–frequency channel estimation problem is first transformed to a set of independent one-dimensional time-domain channel estimation problems using the property that the joint time–frequency correlation function of the channel fading can be represented as the product of the correlation functions in the time and the frequency domains. A robust H_∞ channel estimation algorithm is proposed to estimate the channel fading in the time domain. The H_∞ approach differs from the traditional approach such as the Kalman estimation in the following two respects.

- 1) No *a priori* knowledge of the noise source statistics is required. The only assumption is that the noise has finite energy.
- 2) The estimation criterion is to minimize the worst possible effect in the estimation error (including channel modeling error and additive noise).

These two features make the proposed H_∞ estimation algorithm more appropriate for practical OFDM systems where there is significant uncertainty in the statistics of noise and channel fading. Since the proposed H_∞ algorithm has an observer structure similar to that of the Kalman algorithm, the implementation complexity is similar to that of the Kalman algorithm. For this reason, the Kalman algorithm will be used as the benchmark for performance comparison. Simulation results show that the proposed H_∞ estimation approach can

Manuscript received April 14, 2002; revised July 20, 2003; accepted August 19, 2003. The editor coordinating the review of this paper and approving it for publication is L. Hanzo. This work was supported by the Canadian Institute for Telecommunications Research (CITR) under the NCE program of the Government of Canada.

The authors are with the Centre for Wireless Communications, Department of Electrical and Computer Engineering, University of Waterloo, Waterloo, ON N2L 3G1, Canada (e-mail: jcai@bbr.uwaterloo.ca; xshen@bbr.uwaterloo.ca; jwmark@bbr.uwaterloo.ca).

Digital Object Identifier 10.1109/TWC.2004.837295

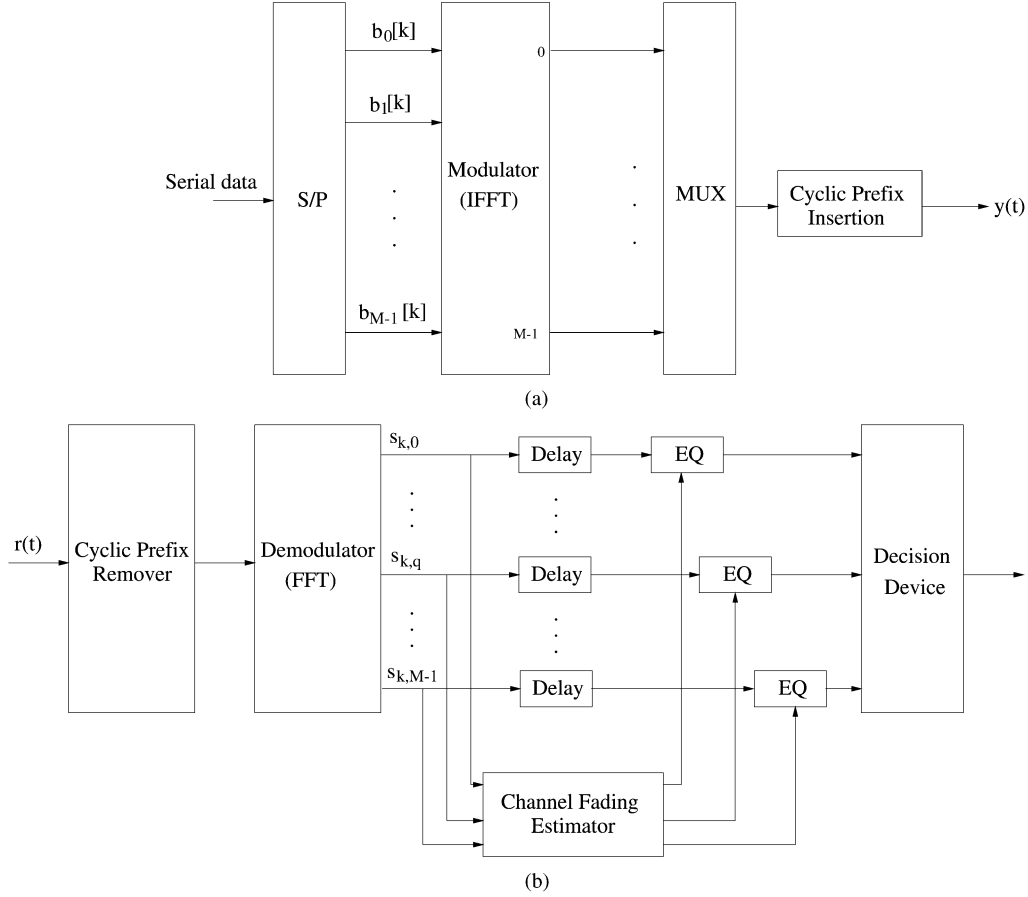


Fig. 1. Transceiver structure of the MC-CDMA system. (a) The transmitter structure. (b) The receiver structure.

improve both the estimation error and bit error rate (BER) performance compared to the Kalman estimation approach.

The remainder of this paper is organized as follows. Section II presents the OFDM system model used in the derivation of the H_∞ estimation algorithm. In Section III, the two-dimensional joint time–frequency domain channel estimation problem in the OFDM system is decomposed and represented by one-dimensional time-domain estimation problems. Section IV presents the H_∞ algorithm for channel estimation in the OFDM system. In Section V, the performance of the H_∞ estimation algorithm is evaluated by simulation in terms of mean-square-error and BER. Conclusions of this paper are given in Section VI.

II. SYSTEM MODEL

Fig. 1 shows the structure of an OFDM transceiver. The serial data at the input is a sequence of samples occurring at interval T_s . At the transmitter [Fig. 1(a)], the high-rate serial input data sequence is first serial-to-parallel (S/P) converted into M low-rate parallel streams in order to increase the symbol duration to $T = MT_s$. The low-rate streams, represented by the symbols $b_m[k]$, $m = 0, 1, \dots, M-1$, $k = 1, 2, \dots$, are modulated onto different subcarriers. In order to eliminate interference between parallel data streams, each of the low-rate data streams is modulated onto a distinct subcarrier belonging to an orthogonal set with subcarrier spacing $1/T$. The parallel streams are then multiplexed and a cyclic prefix is added to eliminate the effect of ISI. Thus, the signal transmitted during the k th symbol interval $y(t)$

can be written as

$$y(t) = \sum_{m=0}^{M-1} b_m[k] e^{j2\pi m t/T}, \quad -\Psi + kT \leq t \leq (k+1)T \quad (1)$$

where $b_m[k]$ is the k th data symbol of the m th stream, M is the total number of subcarriers, and Ψ is the length of the guard interval.

The transmitted signal $y(t)$ passes through the wireless channel which introduces signal distortion and additive noise. The wireless channel can be modeled as a multipath frequency-selective fading channel using a tapped-delay line with time-varying coefficients and fixed tap spacing [13], which can be represented as

$$h(t, \tau) = \sum_{l=0}^{\chi} h_l(t) \delta(\tau - \tau_l) \quad (2)$$

where $h_l(t)$ and τ_l are the complex amplitude and delay of the l th path, respectively. $\chi+1$ is the total number of taps. τ_χ defines the maximum multipath delay spread. For OFDM to be effective, the length of the cyclic prefix Ψ should be larger than the maximum multipath delay spread of the channel. In this paper, $h_l(t)$ is modeled as a wide-sense stationary uncorrelated scattering (WSSUS) process, which has the following correlation function:

$$\begin{aligned} \phi_h(\Delta t) &\triangleq E[h_l(t) h_l^*(t - \Delta t)] \\ &= \sigma_l^2 \phi_t(\Delta t) \end{aligned} \quad (3)$$

where $*$ denotes complex conjugation, σ_l^2 is the variance of the channel fading at path l , which is determined by the power delay profile of the channel and satisfies $\sum_{l=0}^X \sigma_l^2 = 1$, and $\phi_t(\Delta t)$ is the normalized correlation function.

The received signal $r(t)$ in the k th symbol duration can be expressed as

$$\begin{aligned} r(t) &= \int h(t, \tau) y(t - \tau) d\tau \\ &= \sum_{l=0}^X h_l(t) y(t - \tau_l) + n(t) \end{aligned} \quad (4)$$

where $n(t)$ is the background noise.

At the receiver [Fig. 1(b)], the received signal is first demodulated after cyclic prefix removal. For practical implementation, modulation and demodulation can be achieved by inverse fast Fourier transform (IFFT) and fast Fourier transform (FFT), respectively. Channel estimation is applied to obtain the estimates of channel fading in each subcarrier such that coherent detection can be achieved. Delay blocks are introduced to synchronize the outputs of the demodulator and channel estimator. In Fig. 1(b), the second index q at the output of the demodulator refers to the q th subcarrier, and $s_{k,q}$ is the output for the q th subcarrier in the k th symbol interval. By assuming that the channel impulse response is quasi-static during the k th symbol interval so that $h(t) \approx h(kT)$ for $kT \leq t < (k+1)T$, the intercarrier interference can be neglected compared to the background noise. Thus, the q th subcarrier output, $s_{k,q}$, $q \in \{0, 1, \dots, M-1\}$, from the demodulator can be expressed as

$$\begin{aligned} s_{k,q} &= \frac{1}{T} \int_{kT}^{(k+1)T} \left[\sum_{l=0}^X h_l(kT) \right. \\ &\quad \times \left. \sum_{m=0}^{M-1} b_m[k] e^{j2\pi m(t-\tau_l)/T} + n(t) \right] e^{-j2\pi q t/T} dt \\ &= \frac{1}{T} \sum_{l=0}^X h_l(kT) \sum_{m=0}^{M-1} b_m[k] e^{-j2\pi m \tau_l/T} \\ &\quad \times \int_{kT}^{(k+1)T} e^{j2\pi(m-q)t/T} dt \\ &\quad + \frac{1}{T} \int_{kT}^{(k+1)T} n(t) e^{-j2\pi q t/T} dt \\ &= c_{k,q} H_{k,q} + v_{k,q} \end{aligned} \quad (5)$$

where

$$\begin{aligned} c_{k,q} &= b_q[k] \\ H_{k,q} &= \sum_{l=0}^X h_l(kT) e^{-j2\pi q \tau_l/T} \\ v_{k,q} &= \frac{1}{T} \int_{kT}^{(k+1)T} n(t) e^{-j2\pi q t/T} dt. \end{aligned} \quad (6)$$

If the channel fading characterized by $H_{k,q}$ were known, then coherent detection and optimum diversity combining would be achievable at the receiver. However, $H_{k,q}$ is time varying and

usually unknown. Hence, an effective channel estimation algorithm is needed to accurately estimate the channel fading parameter $H_{k,q}$, given $s_{i,q}$, $i \leq k$ and $q = 0, 1, \dots, M-1$.

III. JOINT TIME-FREQUENCY DOMAIN CHANNEL ESTIMATION

Decision-directed [14] and pilot-assisted [15] approaches are two of the most commonly used channel estimation algorithms. Because of the error propagation inherent in the decision-directed approach, the pilot-assisted scheme is preferred. Fig. 2 shows the pilot pattern used in this paper, where the known pilot symbols are inserted in every D_t OFDM symbols and D_f subcarriers. In general, the values of D_t and D_f may significantly affect the estimation performance and should be selected properly [16]–[18]. Without loss of generality, let

$$c_{k,q} = 1, \quad k \in M_t, \quad q \in M_f$$

where M_t and M_f are the sets of pilot positions in the time and frequency domains, respectively. Then, (5) becomes

$$s_{k,q} = H_{k,q} + v_{k,q}, \quad k \in M_t, \quad q \in M_f. \quad (7)$$

Since the $H_{k,q}$ are correlated for different k s and q s, a proper channel estimation algorithm should be carried out jointly in both the time and frequency domains. Directly solving this two-dimensional estimation problem is very difficult. In the following, based on the separation property of the time-frequency correlation function of the channel fading, the two-dimensional estimation problem is decomposed to one-dimensional time-domain estimation problems, which greatly simplifies the original one.

From (3) and (6), the correlation function of the fading channel $\{H_{k,q}, k \in M_t \text{ and } q \in M_f\}$ for different times and subcarriers can be written as [5]

$$\begin{aligned} \phi_H[m, n] &\triangleq E [H_{k,q} H_{k-mD_t, q-nD_f}^*] \\ &= E \left[\sum_{l=0}^X h_l(kT) e^{-j2\pi q \tau_l/T} \right. \\ &\quad \times \left. \sum_{l'=0}^X h_{l'}^*(kT - mD_t T) e^{j2\pi(q-nD_f)\tau_{l'}/T} \right] \\ &= \phi_t(mD_t T) \sum_{l=0}^X \sigma_l^2 e^{-j2\pi n D_f \tau_l/T} \\ &= \phi_t[m] \phi_f[n] \end{aligned} \quad (8)$$

where

$$\begin{aligned} \phi_t[m] &\triangleq \phi_t(mD_t T) \\ \phi_f[n] &\triangleq \sum_{l=0}^X \sigma_l^2 e^{-j2\pi n D_f \tau_l/T}. \end{aligned}$$

Equation (8) indicates that the time-frequency correlation function of the fading channel in the OFDM system can be represented as the product of the correlation functions in the time domain and in the frequency domain.

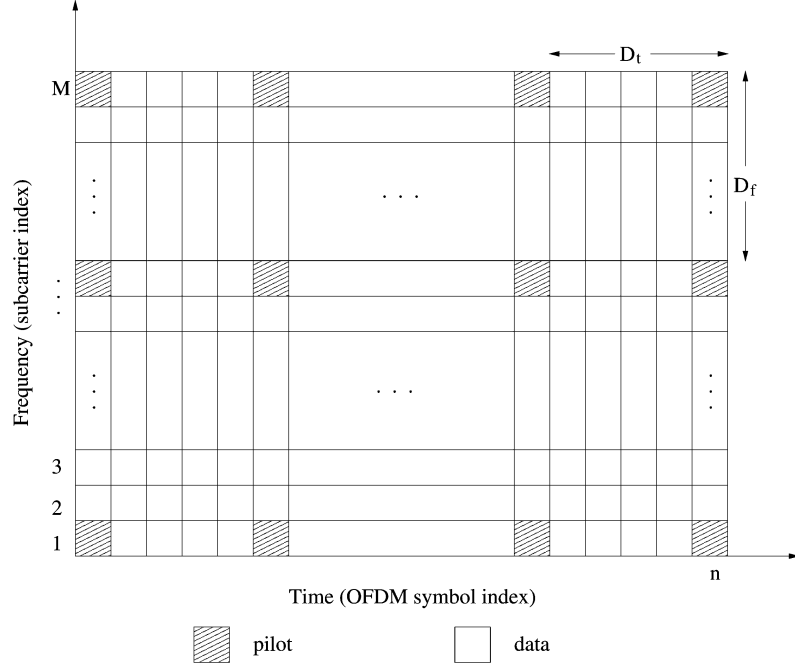


Fig. 2. Configuration of pilot arrangement.

Let

$$\phi_f[q] = \begin{bmatrix} \phi_f[q] \\ \vdots \\ \phi_f[0] \\ \vdots \\ \phi_f[-K+1+q] \end{bmatrix}$$

$$\Phi_f = [\phi_f[0] \quad \phi_f[1] \quad \cdots \quad \phi_f[K-1]]$$

where $K = (M)/(D_f)$ is the number of pilot symbols in the frequency domain given the symbol time instant $k \in M_t$. Assuming that Φ_f is diagonalizable, the eigendecomposition of Φ_f is

$$\Phi_f = \mathbf{U}^H \mathbf{D} \mathbf{U} \quad (9)$$

where the superscript H denotes Hermitian transposition, $\mathbf{U}$ is a unitary matrix consisting of the eigenvectors of Φ_f , and $\mathbf{D}$ is a $K \times K$ diagonal matrix with the diagonals consisting of K_0 ($K_0 \leq K$) nonzero eigenvalues $d_l, l = 0, 1, \dots, K_0 - 1$, and $K - K_0$ zeros. In the absence of knowledge of the channel fading statistics, we choose $K_0 = \lceil \tau_\chi / T_s \rceil$ [5], where $\lceil x \rceil$ denotes the ceiling function. Alternatively, K_0 may be determined using the approach in [19]. Let

$$\begin{aligned} \bar{\mathbf{s}}_k &= [s_{k,0} \quad s_{k,D_f} \quad \cdots \quad s_{k,(K-1)D_f}] \mathbf{U}^H \\ \mathbf{g}_k &= [H_{k,0} \quad H_{k,D_f} \quad \cdots \quad H_{k,(K-1)D_f}] \mathbf{U}^H \\ \bar{\mathbf{v}}_k &= [v_{k,0} \quad v_{k,D_f} \quad \cdots \quad v_{k,(K-1)D_f}] \mathbf{U}^H. \end{aligned}$$

From (7) and (8), we have

$$\begin{cases} \bar{s}_{k,l} = g_{k,l} + \bar{v}_{k,l}, \quad l = 0, 1, \dots, K_0 - 1 \\ \phi_{g,l}[m] \triangleq E[g_{k,l} g_{k-l-mD_t,l}^*] = \phi_t[m] \mathbf{U}_l \Phi_f \mathbf{U}_l^H = d_l \phi_t[m] \\ \sigma_v^2 \triangleq E[|\bar{v}_{k,l}|^2] = E[|v_{k,l}|^2] = \sigma_v^2 \end{cases} \quad (10)$$

where $\bar{s}_{k,l}$, $g_{k,l}$, and $\bar{v}_{k,l}$ are the l th elements of $\bar{\mathbf{s}}_k$, $\mathbf{g}_k$, and $\bar{\mathbf{v}}_k$, respectively; $\mathbf{U}_l$ is the l th row of $\mathbf{U}$. Since the columns of $\mathbf{U}$ form a unitary system

$$E[g_{k,l} g_{k-l-i}^*] = \mathbf{U}_l \Phi_f \mathbf{U}_{l-i}^H = d_l \mathbf{U}_l \mathbf{U}_{l-i}^H = 0, \quad \text{for } i \neq 0. \quad (11)$$

Equation (11) indicates that given time instant k , the $g_{k,l}$ are uncorrelated for different l , i.e., the estimate of $g_{k,l}$ only depends on the observation $\bar{s}_{k',l}, k' \leq k$. In other words, the original joint time-frequency channel fading estimation problem can be transformed to K_0 one-dimensional time-domain estimation problems shown in (10). Fig. 3 shows the derived channel estimator structure, where the observation vector $[s_{k,0}, s_{k,D_f}, \dots, s_{k,(K-1)D_f}]$ is transformed to vector $\bar{\mathbf{s}}_k = [\bar{s}_{k,0}, \bar{s}_{k,1}, \dots, \bar{s}_{k,K-1}]$ by the matrix $\mathbf{U}^H$. Then, $\{g_{k,l}, l = 0, 1, \dots, K_0 - 1\}$ can be estimated by K_0 one-dimensional time-domain estimators. Let the outputs of the K_0 estimators and $K - K_0$ zeros form the vector $\hat{\mathbf{g}}_k = [\hat{g}_{k,0}, \dots, \hat{g}_{k,K_0-1}, 0, \dots, 0]$. The estimates of $H_{k,lD_f}, l = 0, 1, \dots, K - 1$, can be obtained by the inverse transforming $\hat{\mathbf{g}}_k$ using matrix $\mathbf{U}$ [5]. Given the estimate of $H_{k,l}$ at each pilot position, $H_{k,l}, \forall l \in \{0, 1, \dots, M - 1\}$, can be obtained by interpolation.

For time-domain estimation, it is well known that the low-pass slow-fading channel $g_{k,l}$ in (10) can be approximated by an autoregressive (AR) process of the form [20], [21]

$$g_{k,l} = \sum_{i=1}^n a_{i,l} g_{k-iD_t,l} + w_{k,l} \quad (12)$$

where n , $a_{i,l}$, and $w_{k,l}$ denote the order, the coefficient (tap-gain parameter), and the model noise, respectively. Because the channel fading $g_{k,l}$ is a stationary stochastic process and $w_{k,l}$ is a white noise, the tap gain $a_{i,l}$ and the variance of $w_{k,l}$ are

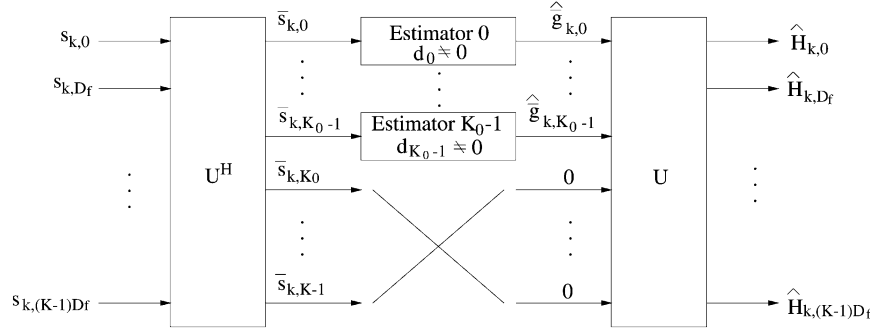


Fig. 3. Joint time-frequency channel estimator for OFDM system.

time-invariant. Without loss of generality, let the zeroth time-domain estimator be the reference and omit the second index l . From (10) and (12), the one-dimensional time-domain channel fading estimation problem can be formulated by the following state-space model:

$$\mathbf{X}_k = \mathbf{A}\mathbf{X}_{k-1} + \mathbf{B}w_k \quad (\text{state equation}) \quad (13)$$

$$\bar{s}_k = \mathbf{C}\mathbf{X}_k + \bar{v}_k \quad (\text{measurement equation}) \quad (14)$$

where

$$\mathbf{X}_k = [g_{k-(n-1)D_t}, g_{k-(n-2)D_t}, \dots, g_k]^T$$

$$\mathbf{A} = \begin{bmatrix} 0 & 1 & 0 & \cdots & 0 & 0 \\ 0 & 0 & 1 & \cdots & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & \cdots & 0 & 1 \\ a_n & a_{n-1} & a_{n-2} & \cdots & a_2 & a_1 \end{bmatrix}$$

$$\mathbf{C} = [0, 0, \dots, 0, 1]$$

$$\mathbf{B} = [0, 0, \dots, 0, 1]^T$$

the superscript T denotes matrix transposition and $\mathbf{A}$ is the channel state transition matrix. If the channel correlation function $\phi_g[m]$ in (10) is known, the tap gain parameter a_i and the variance of w_k can be calculated using the Yule-Walker equations [22]. If the variances of background noise $\bar{v}_k$ is also known, the optimal minimum-error-variance-based estimation algorithms, such as the Kalman filter, can be applied to estimate $\mathbf{X}_k$. However, the severity of the channel impairments depends on whether it is indoor or outdoor, urban or suburban [5]. In practice, the channel correlation function $\phi_g[m]$ and the variance of the background noise are not known *a priori*. The known variance assumptions may provide an estimate that is highly vulnerable to statistical estimation errors, i.e., a small number of measurement errors may have a large effect on the resultant estimate. In the next section, an H_∞ -based channel estimation algorithm for the OFDM system, where knowledge of the variances of w_k and $\bar{v}_k$ is not needed, is presented. For comparison purposes, we first briefly review the Kalman estimation algorithm.

IV. CHANNEL ESTIMATION ALGORITHMS

Impairments in a wireless channel are unknown and most likely time-variant. Methods that do not depend on precise

knowledge of the channel characteristics should be more effective and robust for performing the channel estimation. The designs of channel estimators in which the estimator gains are optimized using a minimum error variance criterion (the Kalman filtering approach) and a minimum estimation error spectrum criterion (the H_∞ filtering approach) are presented. The Kalman approach is a covariance minimization problem while the H_∞ approach is a minimization problem where the maximum “energy” of the estimation error over all disturbances is minimized.

A. Kalman Estimation Algorithm: A Brief Review

Assume that both model noise w_k and background noise $\bar{v}_k$ in (13) and (14) are uncorrelated white Gaussian processes with zero mean and variances

$$E\{w_k w_k^*\} = W$$

$$E\{\bar{v}_k \bar{v}_k^*\} = V.$$

The design objective of the Kalman estimation algorithm is to determine the optimal estimate $\hat{g}_k$ at time k based on the observation $\{\bar{s}_i\}$ ($1 \leq i \leq k$) such that the error covariance

$$\varepsilon_k = E\{e_k e_k^H\} \quad (15)$$

is minimized, where the estimation error e_k is given by

$$e_k = g_k - \hat{g}_k. \quad (16)$$

For the state-space model (13) and (14), the Kalman estimation algorithm is given by

$$\hat{\mathbf{X}}_k = \mathbf{A}\hat{\mathbf{X}}_{k-1} + \mathbf{K}_k[\bar{s}_k - \mathbf{C}\mathbf{A}\hat{\mathbf{X}}_{k-1}] \quad (17)$$

with initial condition $\hat{\mathbf{X}}_0 = [0]_{n \times 1}$. The estimator gain and error covariance equations are

$$\mathbf{K}_k = \mathbf{P}_{k|k-1}\mathbf{C}[V + \mathbf{C}\mathbf{P}_{k|k-1}\mathbf{C}^T]^{-1} \quad (18)$$

$$\mathbf{P}_{k|k-1} = \mathbf{A}\mathbf{P}_{k-1}\mathbf{A}^T + \mathbf{B}\mathbf{W}\mathbf{B}^T \quad (19)$$

$$\mathbf{P}_k = [\mathbf{I} - \mathbf{K}_k\mathbf{C}]\mathbf{P}_{k|k-1} \quad (20)$$

where $\mathbf{K}_k$ is the Kalman gain vector, $\mathbf{P}_{k|k-1} = E[(\mathbf{X}_k - \hat{\mathbf{X}}_{k|k-1})^H(\mathbf{X}_k - \hat{\mathbf{X}}_{k|k-1})]$ is the *a priori* error covariance matrix, $\mathbf{P}_k = E[(\mathbf{X}_k - \hat{\mathbf{X}}_k)^H(\mathbf{X}_k - \hat{\mathbf{X}}_k)]$ is the *a posteriori* error

covariance matrix, with initial condition $\mathbf{P}_0 = [0]_{n \times n}$, and $\mathbf{I}$ is an $n \times n$ identity matrix.

B. H_∞ Estimation Algorithm

Consider the state-space model (13)–(14). We shall not make any assumptions on the disturbances w_k and $\bar{v}_k$, except that they have finite energy. The finite energy assumption is reasonable since in any practical system, both w_k and $\bar{v}_k$ are samples of bandlimited noise process. Let $z_k = \xi \mathbf{X}_k$, where ξ is a $1 \times n$ linear transformation operator. Thus, unlike the Kalman estimation approach, the H_∞ estimation approach achieves estimation using a linear combination of the channel state variables. Let $\hat{z}_k$ be the estimate of z_k , and the estimation error be

$$e_k \triangleq z_k - \hat{z}_k. \quad (21)$$

The design criterion of the H_∞ estimator is to provide a uniformly small estimation error for any $w_k, \bar{v}_k$, and initial condition $\mathbf{X}_0$. The measure of performance is defined as the transfer operator which transforms the $w_k, \bar{v}_k$ and the uncertainty of the initial condition $\mathbf{X}_0$ to the estimation error e_k . The objective function is

$$J \triangleq \frac{\sum_{i=0}^{\infty} |e_i|_Q^2}{|\mathbf{X}_0 - \hat{\mathbf{X}}_0|_{\mathbf{P}_0^{-1}}^2 + \sum_{i=0}^{\infty} \left\{ |\bar{v}_i|_{V_H^{-1}}^2 + |w_i|_{W_H^{-1}}^2 \right\}} \quad (22)$$

where $|\mathbf{x}|_G^2 \triangleq \mathbf{x}^H \mathbf{G} \mathbf{x}$, $\hat{\mathbf{X}}_0$ is an *a priori* estimate of $\mathbf{X}_0$, $(\mathbf{X}_0 - \hat{\mathbf{X}}_0)$ represents unknown initial condition error, and $Q \geq 0, \mathbf{p}_0 > 0, W_H > 0$, and $V_H > 0$ are weighting parameters. $\mathbf{p}_0$ denotes a positive definite matrix that reflects *a priori* knowledge on how close the initial guess $\hat{\mathbf{X}}_0$ is to $\mathbf{X}_0$. W_H and V_H are weighting variables which are left to the choice of the designer and depend on the performance requirement. In practical systems, the values of W_H and V_H can be chosen as the estimates of the covariances of the corresponding noises. The optimal estimate of z_k among all possible $\hat{z}_k$ (i.e., the worst case performance measure) should satisfy

$$\|J\|_\infty \triangleq \sup_{\bar{v}_k, w_k, \mathbf{X}_0} J \leq \gamma^{-1} \quad (23)$$

where “sup” stands for supremum and $\gamma (>0)$ is a prescribed level of noise attenuation. The value that γ can take is discussed in the next section. Equation (23) shows that the H_∞ optimal estimator guarantees the smallest estimation error energy over all possible disturbances with finite energy.

The discrete-time H_∞ estimation can be interpreted as a minimax problem where the strategy is to play the estimate $\hat{z}_k$ against the exogenous inputs $w_k, \bar{v}_k$ and the uncertainty of the initial state $\mathbf{X}_0$ [23]. Using $z_k = \xi \mathbf{X}_k$ and $\hat{z}_k = \xi \hat{\mathbf{X}}_k$, the performance criterion can be equivalently represented as

$$\min_{\hat{\mathbf{X}}_k} \max_{\bar{v}_k, w_k, (\mathbf{X}_0)} J = -\frac{1}{2} \gamma^{-1} |\mathbf{X}_0 - \hat{\mathbf{X}}_0|_{\mathbf{P}_0^{-1}}^2 + \frac{1}{2} \sum_{i=0}^{\infty} [|\mathbf{X}_k - \hat{\mathbf{X}}_k|_Q^2 - \gamma^{-1} (|w_i|_{W_H^{-1}}^2 + |\bar{v}_i|_{V_H^{-1}}^2)] \quad (24)$$

where $\bar{\mathbf{Q}} = \xi^T Q \xi$, and “min” and “max” stand for minimization and maximization, respectively. In (24), the maximization is used to calculate the worst case of J over all disturbance, and then, the estimate is obtained by minimizing the worst case of J . This minimax problem can be solved by using a game theory approach [23]–[25]. For the state-space model (13) and (14) with the performance criterion (24), there exists an H_∞ estimator for z_k if and only if there exists a stabilizing symmetric positive definite solution $\mathbf{P}_k$ to the following discrete-time Riccati type equation:

$$\begin{aligned} \mathbf{P}_{k+1} &= \mathbf{A} \mathbf{P}_k (\mathbf{I} - \gamma \bar{\mathbf{Q}} \mathbf{P}_k + \mathbf{C}^T V_H^{-1} \mathbf{C} \mathbf{P}_k)^{-1} \mathbf{A}^T \\ &\quad + \mathbf{B} W_H \mathbf{B}^T \\ \mathbf{P}_0 &= \mathbf{p}_0 \end{aligned} \quad (25)$$

where $\mathbf{p}_0$ is the initial condition. If a solution $\mathbf{P}_k$ exists, then the H_∞ estimator is given by

$$\hat{z}_k = \xi \hat{\mathbf{X}}_k, \quad k = 1, 2, 3, \dots \quad (26)$$

where

$$\hat{\mathbf{X}}_k = \mathbf{A} \hat{\mathbf{X}}_{k-1} + \mathbf{G}_k (\bar{s}_k - \mathbf{C} \mathbf{A} \hat{\mathbf{X}}_{k-1}), \quad \hat{\mathbf{X}}_0 = [0]_{n \times 1} \quad (27)$$

and $\mathbf{G}_k$ is the gain of the H_∞ estimator given by

$$\mathbf{G}_k = \mathbf{P}_k (\mathbf{I} - \gamma \bar{\mathbf{Q}} \mathbf{P}_k + \mathbf{C}^T V_H^{-1} \mathbf{C} \mathbf{P}_k)^{-1} \mathbf{C}^T V_H^{-1}. \quad (28)$$

Comparing the Kalman estimation algorithm (17)–(20) and the H_∞ estimation algorithm (25)–(28), we can observe the following.

- 1) The Kalman estimation algorithm minimizes the covariance of the estimation error of the state vector $\mathbf{X}_k$ based on the $\{\bar{s}_i\}$ ($1 \leq i \leq k$). The algorithm is independent of ξ .
- 2) The H_∞ estimation algorithm gives the optimal estimate of $\xi \mathbf{X}_k$ based on the $\{\bar{s}_i\}$ ($1 \leq i \leq k$) such that the effect of the worst disturbances on the estimation error is minimized.
- 3) The H_∞ and Kalman estimation algorithms have similar observer structure.

Let the weighting parameters (W_H, V_H) and $\mathbf{p}_0$ of the H_∞ estimation algorithm be the same as the covariances (W, V) and $\mathbf{P}_0$ of the Kalman estimation algorithm. In the limiting case, where the parameter $\gamma \rightarrow 0$, the H_∞ estimation algorithm reduces to a Kalman estimation algorithm.

The following observations reveal a glimpse of the implementation complexity of the H_∞ algorithm relative to the Kalman and MMSE algorithms.

- 1) From the similar observer structure between the proposed H_∞ and the Kalman estimation algorithms, the H_∞ estimator has a similar hardware structure and computation complexity as the Kalman estimator.
- 2) For the H_∞ estimation algorithm, different estimation results can be obtained with different vector ξ . For example, if we choose $\xi = [1, 0, \dots, 0]_{1 \times n}$, the H_∞ estimation algorithm is designed to obtain the optimal estimation of $g_{k-(n-1)D_t}$. The estimate $\hat{g}_{k-(n-1)D_t}$

should give a better estimation of channel fading $g_{k-(n-1)D_t}$ at the k th instant since the estimation is based on the $\{\bar{s}_i\}$, $1 \leq i \leq k$. This estimation is equivalent to the fixed-lag smoothing problem. The only difference from the traditional fixed-lag smoothing problem is that no additional computation is required in this case.

- 3) Although the MMSE estimation algorithm proposed in [5] can endure some mismatch on the correlation function of the channel fading, information on coherence bandwidth of the channel fading and the variance of the background noise is still required. Obtaining this accurate information may greatly increase the complexity of the receiver design. For the proposed H_∞ algorithm, the inherent robustness reduces the dependence of the estimation performance on the accuracy of the parameter estimation, which significantly reduces the complexity of the receiver design. In addition, because of the recursive property of the H_∞ algorithm, the complexity on the matrix computation is much less than that in the MMSE algorithm since there is no need to store a large number of past measurements.

C. γ Value Determination

A necessary and sufficient condition for the existence of the H_∞ estimator is that the discrete-time Riccati equation (25) has a positive-definite solution $\mathbf{P}_k$. Thus, the parameter γ should be selected carefully to satisfy this constraint. From (25), as long as the parameter γ is small enough, the Riccati equation always has positive definite solutions. On the other hand, in the design criterion (23), it is observed that the larger the γ value, the less effect the interference has on the estimation error. As a result, the γ value at any time instant $k+1$ depends on $\mathbf{P}_k$, $\bar{\mathbf{Q}}$, $\mathbf{C}$, and V_H .

From (25), in order to guarantee $\mathbf{P}_{k+1}$ to be positive definite, it requires

$$\begin{aligned} & \mathbf{P}_k (\mathbf{I} - \gamma \bar{\mathbf{Q}} \mathbf{P}_k + \mathbf{C}^T V_H^{-1} \mathbf{C} \mathbf{P}_k)^{-1} > 0 \\ & \Rightarrow \mathbf{P}_k^{-1} - \gamma \bar{\mathbf{Q}} + \mathbf{C}^T V_H^{-1} \mathbf{C} > 0 \\ & \Rightarrow \gamma \bar{\mathbf{Q}} < \mathbf{P}_k^{-1} + \mathbf{C}^T V_H^{-1} \mathbf{C} \\ & \Rightarrow \gamma^{-1} (\mathbf{P}_k^{-1} + \mathbf{C}^T V_H^{-1} \mathbf{C}) > \bar{\mathbf{Q}} \\ & \Rightarrow \gamma^{-1} \mathbf{I} > \bar{\mathbf{Q}} (\mathbf{P}_k^{-1} + \mathbf{C}^T V_H^{-1} \mathbf{C})^{-1} \\ & \Rightarrow \gamma^{-1} > \max \left\{ \text{eig} \left[\bar{\mathbf{Q}} (\mathbf{P}_k^{-1} + \mathbf{C}^T V_H^{-1} \mathbf{C})^{-1} \right] \right\} \quad (29) \end{aligned}$$

where $\max\{\text{eig}(\mathbf{X})\}$ denotes the maximum eigenvalue of the matrix $\mathbf{X}$.

D. Tap-Gain Parameter Estimation

The channel estimation algorithm proposed in Section IV-B needs the information on the tap-gain parameters, $a_i, i = 1, 2, \dots, n$, of the AR model. In this section, an H_∞ algorithm is proposed to estimate the tap-gain parameters from the observations.

Since the low-pass slow-fading channel g_k can be approximated by an AR model described in (12), from (10), the received signal at the pilot position can be written as

$$\begin{aligned} \bar{s}_k &= g_k + \bar{v}_k \\ &= \sum_{i=1}^n a_i g_{k-iD_t} + w_k + \bar{v}_k \\ &= \sum_{i=1}^n a_i (\bar{s}_{k-iD_t} - \bar{v}_{k-iD_t}) + w_k + \bar{v}_k \\ &= \sum_{i=1}^n a_i \bar{s}_{k-iD_t} + u_k \quad (30) \end{aligned}$$

where $u_k = w_k + \bar{v}_k - \sum_{i=1}^n a_i \bar{v}_{k-iD_t}$. For the stationary stochastic process g_k , $\{a_i, i = 1, 2, \dots, n\}$ is time-invariant. Here, we need to estimate a_i given the observation $\bar{s}_k$. Let

$$\begin{aligned} \boldsymbol{\alpha} &= [a_n, a_{n-1}, \dots, a_1]^T \\ \boldsymbol{\theta}_k &= [\bar{s}_{k-n}, \bar{s}_{k-n+1}, \dots, \bar{s}_{k-1}]^T \quad (31) \end{aligned}$$

and $\hat{\boldsymbol{\alpha}}_k$ be the estimate of $\boldsymbol{\alpha}$ at time instant k . Then the measurement and estimation error equations can be written as

$$\bar{s}_k = \boldsymbol{\theta}_k^T \boldsymbol{\alpha}_k + u_k \quad (32)$$

$$e_k^t = \boldsymbol{\theta}_k^T \boldsymbol{\alpha} - \boldsymbol{\theta}_k^T \hat{\boldsymbol{\alpha}}_k \quad (33)$$

where the superscript t denotes that the error is due to the tap-gain estimation. The performance criterion can be represented as

$$\begin{aligned} \min_{e_k^t} \max_{u_k, \boldsymbol{\alpha}_0} J^t &= -\frac{1}{2} (\gamma^t)^{-1} |\boldsymbol{\alpha} - \hat{\boldsymbol{\alpha}}_0|_{(\mathbf{P}_0^t)^{-1}}^2 \\ &+ \frac{1}{2} \sum_{i=0}^{\infty} \left[|e_k^t|_{(Q^t)}^2 - \gamma^{-1} |u_i|_{(V^t)^{-1}}^2 \right] \quad (34) \end{aligned}$$

where $\hat{\boldsymbol{\alpha}}_0$ is an *a priori* estimate of $\boldsymbol{\alpha}$, and $Q^t, (\mathbf{P}_0^t)$, and V^t are weights. Following a similar approach as in Section IV-B, the H_∞ estimation algorithm to estimate the optimal $\boldsymbol{\alpha}_k$ can be obtained as

$$\begin{aligned} \hat{\boldsymbol{\alpha}}_k &= \hat{\boldsymbol{\alpha}}_{k-1} + \mathbf{K}_k^t (\bar{s}_k - \boldsymbol{\theta}_k^T \hat{\boldsymbol{\alpha}}_{k-1}), \quad \hat{\boldsymbol{\alpha}}_0 = [0]_{n \times 1} \quad (35) \\ \mathbf{K}_k^t &= \mathbf{P}_k^t \left(\mathbf{I} - \gamma^t \boldsymbol{\theta}_k^T Q^t \boldsymbol{\theta}_k \mathbf{P}_k^t + \boldsymbol{\theta}_k^T (V^t)^{-1} \boldsymbol{\theta}_k \mathbf{P}_k^t \right)^{-1} \\ &\quad \times \boldsymbol{\theta}_k^T (V^t)^{-1} \quad (36) \\ \mathbf{P}_{k+1}^t &= \mathbf{P}^t \left(\mathbf{I} - \gamma^t \boldsymbol{\theta}_k^T Q^t \boldsymbol{\theta}_k \mathbf{P}_k^t + \boldsymbol{\theta}_k^T (V^t)^{-1} \boldsymbol{\theta}_k \mathbf{P}_k^t \right)^{-1} \\ \mathbf{P}_0^t &= \mathbf{P}_0^t. \quad (37) \end{aligned}$$

In order to guarantee the existence of the algorithm, γ^t should satisfy (29). In practical systems, the tap-gain parameters can be estimated by transmitting a training sequence with high signal-to-noise ratio (SNR). Simulation results in the next section show that for high SNR training sequences, the estimator can provide fairly accurate estimates of the tap-gains.

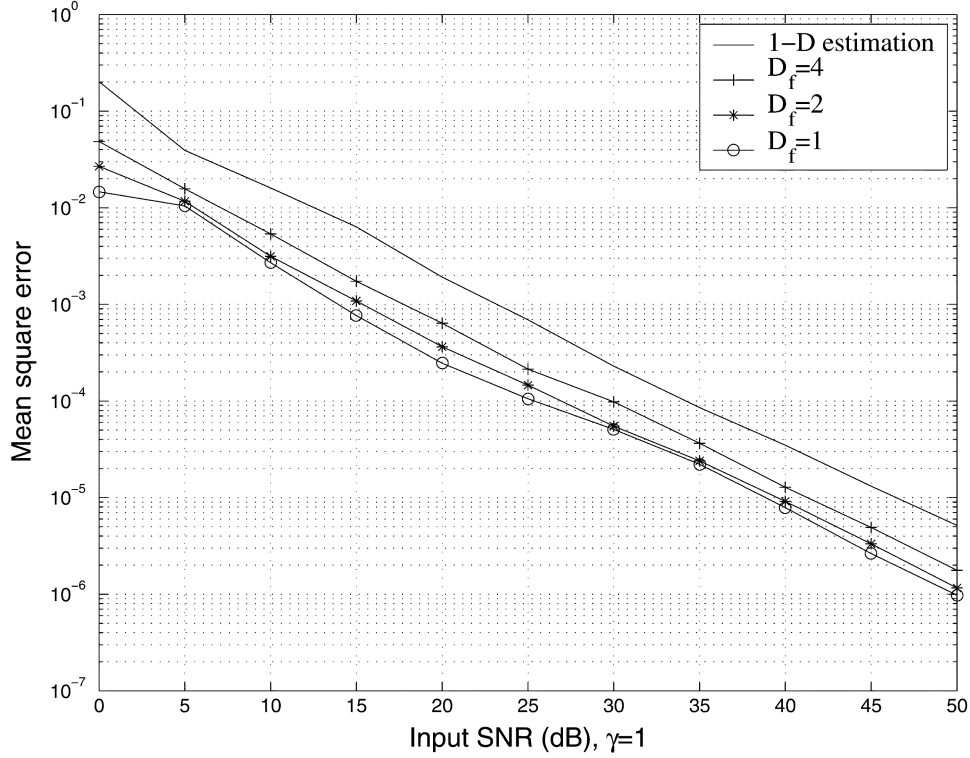


Fig. 4. Performance comparison between one-dimensional estimation and joint two-dimensional estimation.

V. SIMULATION RESULTS AND DISCUSSION

In this section, simulation results are presented to evaluate the performance of channel estimation with both the H_∞ and Kalman approaches.

A. System Parameters

Consider an OFDM system using binary phase-shift keying with 32 subcarriers. The channel used in the simulation is a two-path Rayleigh-fading channel model with delay zero and T_s . The power spectral density satisfies Jakes model, i.e., the time correlation function is of the form

$$\phi_t[m] = J_0(2\pi f_d T_m D_t) \quad (38)$$

where $f_d T$ is the normalized Doppler frequency and is set to 0.05 to characterize a slowly fading channel. The power delay profile is assumed exponentially distributed, i.e.,

$$\sigma_l^2 = \frac{e^{-l/(\chi+1)}}{\sum_{l=0}^{\chi} e^{-l/(\chi+1)}} \quad (39)$$

The background noise is modeled as a zero-mean independent identically distributed complex Gaussian random sequence with variance σ^2 . The signal power is normalized to 1 so that the input SNR is defined as $1/\sigma^2$. The length of the time window n is three and the vector ξ of the H_∞ estimation algorithm is $[1, 0, 0]$. $\gamma = 1$ is obtained from (29). For performance comparison, without loss of generality, we choose $D_t = 1$. Since the focus is robustness of the channel fading estimation algorithm to the errors on W and V , accurate tap-gain parameters $a_i, i = 1, 2, \dots, n$, are used in the simulation. The tap-gain

parameters $a_i, i = 1, 2, \dots, n$, are also estimated based on (35)–(37) by transmitting a training sequence with SNR = 40 dB. It is shown the performance with the estimated tap-gain parameters is similar to that with the accurate tap-gain parameters.

B. Effect of Number of Pilots in the Frequency Domain

Fig. 4 shows the mean-square-error of the H_∞ algorithm with different values of D_f . For performance comparison, the one-dimensional time-domain estimation algorithm proposed in [17], which only uses the time correlation of the channel fading, is also simulated. To make a fair comparison between one-dimensional and two-dimensional algorithms, in our simulation, the one-dimensional H_∞ estimation algorithm is used in place of the one-dimensional least square (LS) algorithm in [17]. The simulation results show that joint estimation in both the time and frequency domains outperforms the one-dimensional time-domain estimation. Decreasing the value of D_f , i.e., increasing the number of pilots in the frequency domain, can further improve the estimation performance. However, further increasing the number of pilots can only yield marginal improvement on the mean-square-error since the improvement saturates at about $D_f = 4$. In the following simulation, without loss of generality, we choose $D_f = 2$.

C. Effect of Input SNR

Fig. 5 shows the mean-square-error versus SNR [no interference (intracell or intercell interference)]. The simulation results show the following.

- 1) With an increase in input SNR, the mean-square-error performance of both the H_∞ and Kalman estimation algorithms improves.

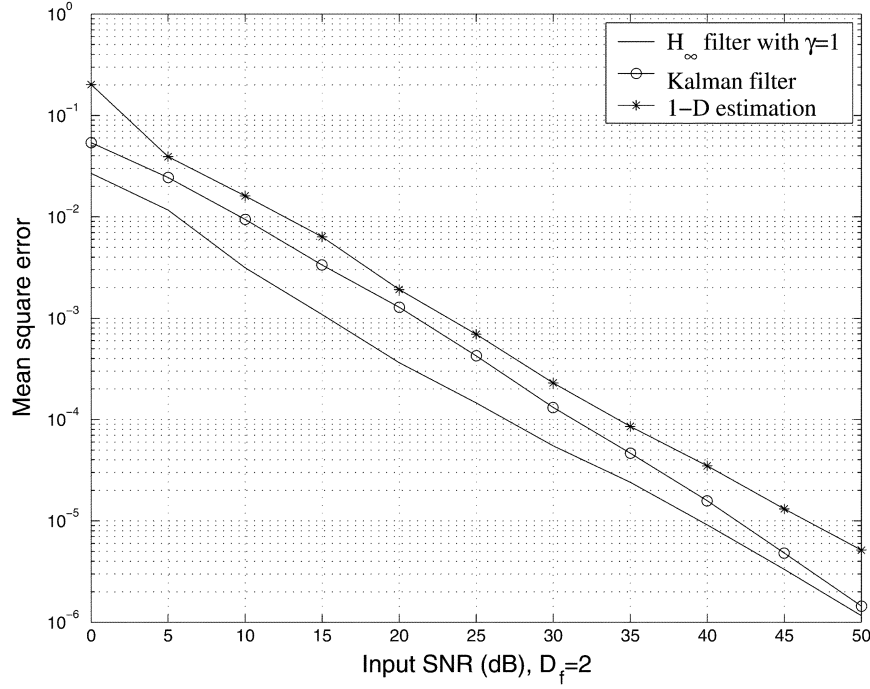


Fig. 5. Mean-square-error performance over different input SNR.

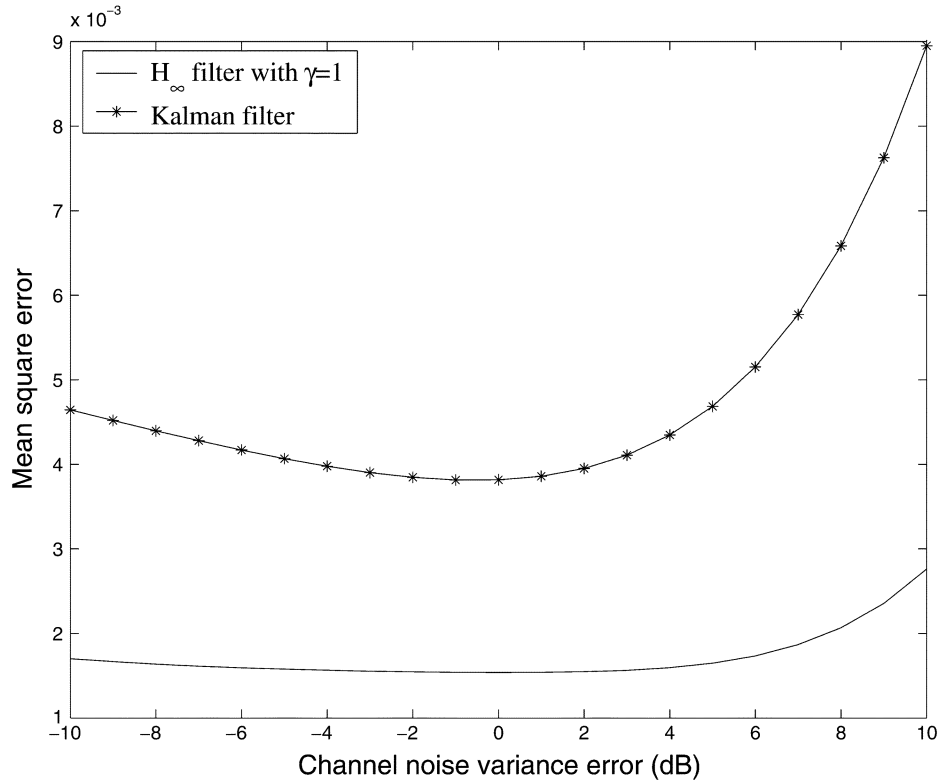


Fig. 6. Effects of errors on background noise covariance V .

- 2) The H_∞ estimation algorithm outperforms the Kalman estimation algorithm over all the SNR range considered.
- 3) At very high SNR, the performance of the H_∞ and Kalman estimation algorithms merges because the signal component tends to swamp out the channel noise.

D. Effect of Model Parameter (V and W) Errors

Figs. 6 and 7 show the effects of the background noise and the model noise covariance errors on the estimation performance, respectively. Note that the accurate values of W and V are used in Figs. 6 and 7, respectively. In the simulation, the input SNR is chosen to be 15 dB. Let the channel noise covariance and

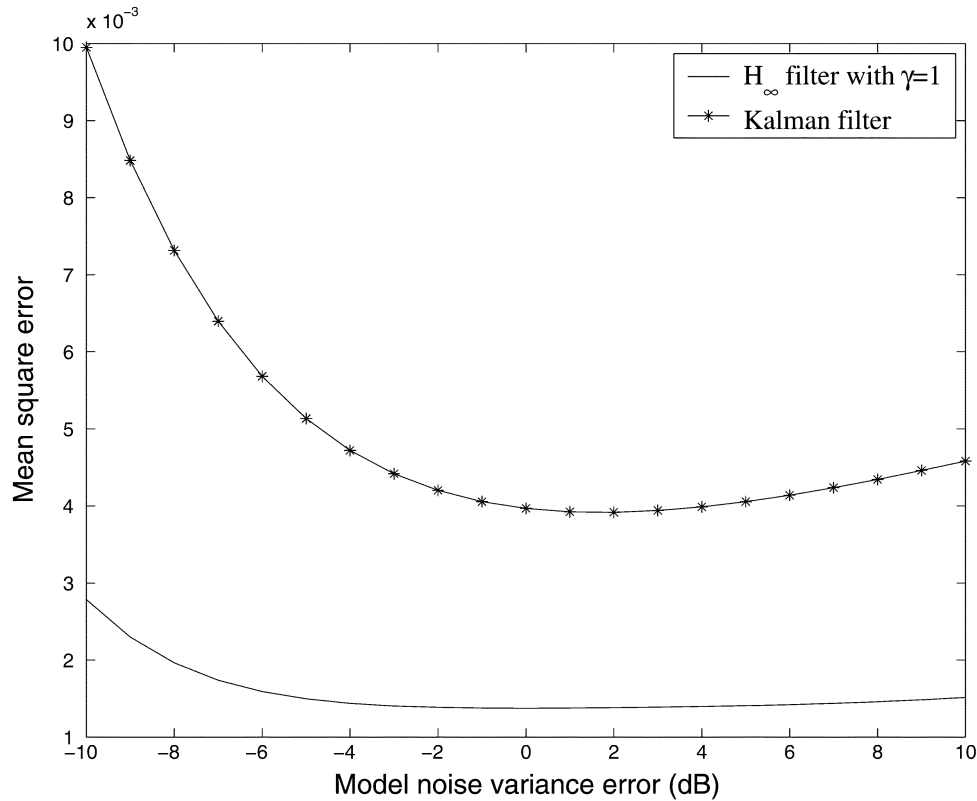


Fig. 7. Effects of errors on model noise covariance W .

the model noise covariance used for estimator design be ρV and ρW , respectively, where ρ is a multiplier to represent the deviation of the design parameters from the true values. In the simulation, ρ takes value in the range from -10 to 10 dB and $\rho = 0$ dB means no deviation. From the figures, it can be seen that model parameter errors can considerably degrade the performance of the Kalman estimation algorithm. The H_∞ estimation algorithm outperforms the Kalman estimation algorithm over the whole error range considered. The larger the error, the larger is the performance gain of the H_∞ algorithm over the Kalman algorithm. Furthermore, as the errors increase, the performance degradation of the H_∞ estimation algorithm is more gradual compared to that of the Kalman estimation algorithm. For example, in Fig. 6, the mean-square-error using the Kalman estimation algorithm changes from 0.0038 at 0 dB to 0.009 at 10 dB, while the mean-square-error using the H_∞ estimation algorithm changes from 0.0015 at 0 dB to 0.0028 at 10 dB. The variation of mean-square-error for the Kalman estimation algorithm is four times larger than that of the H_∞ estimation algorithm. The smaller variation indicates that the H_∞ estimation algorithm is more robust against the parameter errors compared to the Kalman estimation algorithm.

E. BER Performance

At the receiver, the received signal is multiplied by the conjugate of the channel estimate to compensate for the phase offset introduced by the fading channel, and the data symbols are recovered by coherent detection.

Fig. 8 shows the BER performance of the OFDM system using the H_∞ and Kalman channel estimation algorithms. The following is observed.

- 1) The BER performance based on the H_∞ estimation algorithm outperforms that based on the Kalman estimation algorithm over all the SNR range considered. The reason is that the more accurate channel estimate obtained by the H_∞ estimation algorithm can provide more accurate phase information about the channel fading. More accurate phase information can provide better coherent detection performance. For example, at a BER of 10^{-4} , the input SNR of the system with H_∞ estimation is 27.2 dB, while it is 31.7 dB for the system with Kalman estimation. The improvement is 4.5 dB.
- 2) At high SNR, the BER characteristics of both the H_∞ and Kalman estimation algorithms are close to each other. The reason is that, at high SNR, both estimation algorithms can achieve nearly the same channel estimation accuracy.

VI. CONCLUSION

A robust channel estimation algorithm based on the H_∞ approach has been proposed for OFDM wireless communication systems. The proposed H_∞ algorithm minimizes the effect of worst disturbance (including both background noise and channel model noise) on the estimation error and, therefore, is less sensitive to the uncertainty of the channel statistics. Simulation results indicate that the H_∞ estimation algorithm

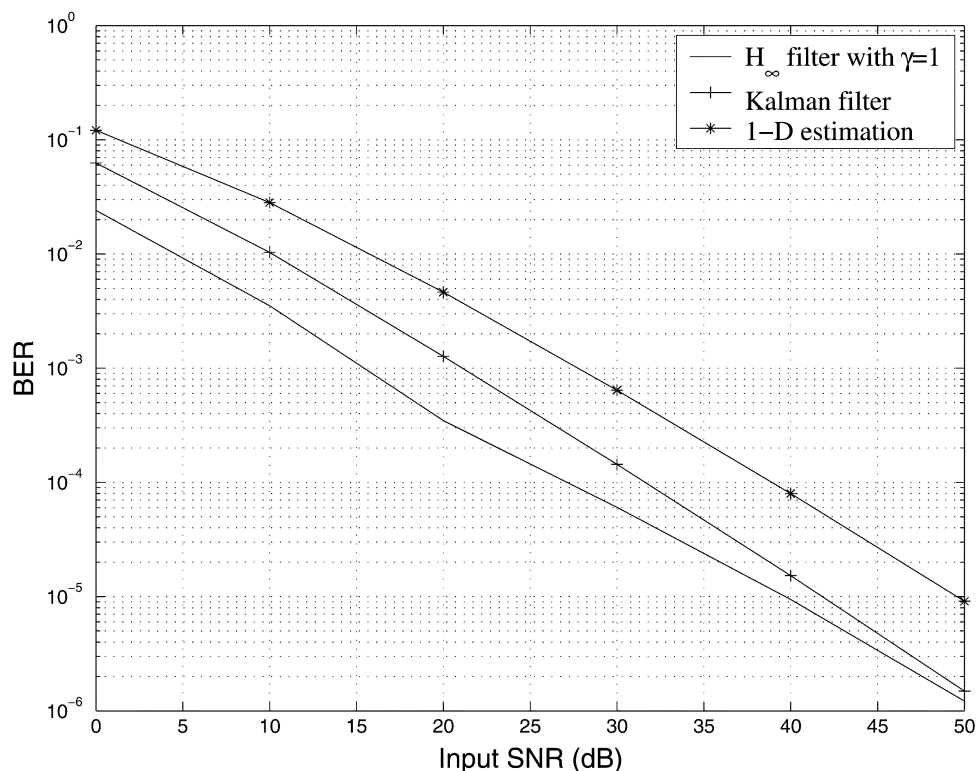


Fig. 8. BER performance comparison between the H_∞ and Kalman estimation algorithms.

has superior performance to the Kalman estimation counterpart, while keeping the similar implementation complexity.

ACKNOWLEDGMENT

The authors wish to thank the anonymous reviewers for their helpful reviews and suggestions.

REFERENCES

- [1] J. A. C. Bingham, "Multicarrier modulation for data transmission: An idea whose time has come," *IEEE Commun. Mag.*, vol. 28, pp. 5–14, May 1990.
- [2] S. B. Weinstein and P. M. Ebert, "Data transmission by frequency-division multiplexing using the discrete Fourier transform," *IEEE Trans. Commun.*, vol. COM-19, pp. 628–634, Oct. 1971.
- [3] L. J. Cimini Jr., "Analysis and simulation of a digital mobile channel using orthogonal frequency division multiplexing," *IEEE Trans. Commun.*, vol. COM-33, pp. 665–675, July 1985.
- [4] V. Mignone and A. Morello, "CD3-OFDM: A novel demodulation scheme for fixed and mobile receivers," *IEEE Trans. Commun.*, vol. 44, pp. 1144–1151, Sept. 1996.
- [5] Y. Li, L. J. Cimini, and N. R. Sollenberger, "Robust channel estimation for OFDM systems with rapid dispersive fading channels," *IEEE Trans. Commun.*, vol. 46, pp. 902–915, July 1998.
- [6] H. Minn and V. K. Bhargava, "An investigation into time-domain approach for OFDM channel estimation," *IEEE Trans. Broadcast.*, vol. 46, pp. 240–248, Dec. 2000.
- [7] P. K. Frenger, N. Arne, and B. Svensson, "Decision-directed coherent detection in multicarrier systems on Rayleigh fading channels," *IEEE Trans. Veh. Technol.*, vol. 48, pp. 490–498, Mar. 1999.
- [8] S. U. H. Qureshi, "An adaptive decision-feedback receiver using maximum-likelihood sequence estimation," in *Proc. IEEE Int. Conf. Commun.*, Seattle, WA, June 1973, pp. 14.10–14.16.
- [9] D. K. Borah and B. D. Hart, "Frequency-selective fading channel estimation with a polynomial time-varying channel model," *IEEE Trans. Commun.*, vol. 47, pp. 862–873, June 1999.
- [10] O. Edfors, M. Sandell, and J. van de Beek, "OFDM channel estimation by singular value decomposition," *IEEE Trans. Commun.*, vol. 46, pp. 931–939, July 1998.
- [11] J. van de Beek, O. Edfors, M. Sandell, S. K. Wilson, and P. O. Börjesson, "On channel estimation in OFDM systems," in *Proc. 45th IEEE Vehicular Technology Conf.*, Chicago, IL, July 1995, pp. 815–819.
- [12] I. R. Petersen and A. V. Savkin, *Robust Kalman Filtering for Signals and Systems with Large Uncertainties*. Boston, MA: Birkhäuser, 1999.
- [13] R. Steele, *Mobile Radio Communications*. New York: IEEE Press, 1992.
- [14] M. J. Omid, S. Pasupathy, and P. G. Gulak, "Joint data and Kalman estimation of fading channel using a generalized Viterbi algorithm," in *Proc. ICC'96*, Dallas, TX, June 1996, pp. 1198–1203.
- [15] P. Schramm and R. R. Muller, "Pilot symbol assisted BPSK on rayleigh fading channels with diversity: Performance analysis and parameter optimization," *IEEE Trans. Commun.*, vol. 46, pp. 1560–1563, Dec. 1998.
- [16] R. V. Nee and R. Prasad, *OFDM for Wireless Multimedia Communications*. Norwood, MA: Artech House, 1999.
- [17] Y. Li, "Pilot-symbol-aided channel estimation for OFDM in wireless systems," *IEEE Trans. Veh. Technol.*, vol. 49, pp. 1207–1215, July 2000.
- [18] P. Hoehner, S. Kaiser, and P. Robertson, "Two-dimension pilot-symbol-aided channel estimation by Wiener filtering," in *Proc. ICASSP 1997*, Munich, Germany, Apr. 1997, pp. 1845–1848.
- [19] H. Minn, D. I. Kim, and V. K. Bhargava, "A reduced complexity channel estimation for OFDM systems with transmit diversity in mobile wireless channels," *IEEE Trans. Commun.*, vol. 50, pp. 799–807, May 2002.
- [20] M. K. Tsatsanis, G. B. Giannakis, and G. Zhou, "Estimation and equalization of fading channels with random coefficients," *Signal Process.*, vol. 53, pp. 211–229, 1996.
- [21] S. M. Kay, *Modern Spectral Estimation: Theory and Application*. Englewood Cliffs, NJ: Prentice-Hall, 1987.
- [22] G. E. P. Box and G. M. Jenkins, *Time Series Analysis, Forecasting and Control*. San Francisco, CA: Holden-Day, 1976.
- [23] X. Shen and L. Deng, "A dynamic system approach to speech enhancement using the H_∞ filtering algorithm," *IEEE Trans. Speech Audio Processing*, vol. 7, pp. 391–399, July 1999.
- [24] U. Shaked and Y. Theodor, " H_∞ -optimal estimation: A tutorial," in *Proc. 31st IEEE CDC*, Tucson, AZ, Dec. 1992, pp. 2278–2286.
- [25] K. M. Nagpal and P. P. Khargonekar, "Filtering and smoothing in an H_∞ setting," *IEEE Trans. Automat. Contr.*, vol. 36, pp. 152–166, Feb. 1991.



Jun Cai received the B.Eng. degree in radio techniques and the M.Eng. degree in communication and information systems from Xi'an Jiaotong University, China, in 1996 and 1999, respectively. He is currently pursuing the Ph.D. degree in electrical and computer engineering, University of Waterloo, ON, Canada.

His research interests include channel estimation, interference cancellation, and resource management in wireless communication systems.



Xuemin (Sherman) Shen (M'97–SM'02) received the B.Sc. degree from Dalian Marine University, China, in 1982 and the M.Sc. and Ph.D. degrees from Rutgers—The State University, New Brunswick, NJ, in 1987 and 1990, respectively, all in electrical engineering.

From 1990 to 1993, he was with Howard University, Washington, D.C., and then with the University of Alberta, Edmonton, AB, Canada. Since 1993, he has been with the Department of Electrical and Computer Engineering, University of Waterloo, ON,

Canada, where he is a full Professor. His research focuses on mobility and resource management in interconnected wireless/wireline networks, stochastic process, and control. He is a coauthor of two books and has publications in communications networks, control, and filtering.

Dr. Shen is an Editor of the IEEE TRANSACTIONS ON WIRELESS COMMUNICATIONS, Associate Editor of the IEEE TRANSACTIONS ON VEHICULAR TECHNOLOGY, as well as three other international journals. He received the Premier's Research Excellence Award from the Province of Ontario for demonstrated excellence of scientific and academic contributions in 2003. He received the Distinguished Performance Award from the Faculty of Engineering, University of Waterloo, for outstanding contributions in teaching, scholarship, and service in 2002. He was the Technical Vice Chair, IEEE Globecom'03 Symposium on Next Generation Networks and Internet. He was Guest Coeditor, IEEE WIRELESS COMMUNICATIONS, Special Issue on 4G Mobile Communication—Toward Open Wireless Architecture, 2003. He was Technical Program Vice Chair, International Symposium on Parallel Architectures, Algorithms, and Networks, 2003. He is a registered Professional Engineer of Ontario, Canada.



Jon W. Mark (M'62–SM'80–F'88–LF'03) received the B.A.Sc. degree from the University of Toronto, ON, Canada, in 1962 and the M.Eng. and Ph.D. degrees from McMaster University, Hamilton, ON, Canada, in 1968 and 1970, respectively, all in electrical engineering.

From 1962 to 1970, he was an Engineer and then Senior Engineer with Canadian Westinghouse Co. Ltd., Hamilton. In 1970 he joined the Department of Electrical and Computer Engineering, University of Waterloo, ON, where he is currently a Distinguished

Professor Emeritus. He was Department Chairman during 1984–1990. In 1996 he established the Centre for Wireless Communications at the University of Waterloo and is currently its Founding Director. He was on sabbatical leave at the IBM T. J. Watson Research Center, Yorktown Heights, NY, as a Visiting Research Scientist (1976–1977); AT&T Bell Laboratories, Murray Hill, NJ, as a Resident Consultant (1982–1983); Laboratoire MASI, Université Pierre et Marie Curie, Paris, France, as an Invited Professor (1990–1991); and the Department of Electrical Engineering, National University of Singapore, as a Visiting Professor (1994–1995). He previously worked in the areas of adaptive equalization, spread-spectrum communications, and antijamming secure communication over satellites. His current research interests are in broadband and wireless communication networks, including network architecture, routing, and control, and resource and mobility management in wireless and hybrid wireless/wireline communication networks. He is currently an Editor of *Wireless Networks* and an Associate Editor of *Telecommunication Systems*.

Dr. Mark was an Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS during 1983–1989. He was Technical Program Chairman of INFOCOM'89. He was a member of the Inter-Society Steering Committee of the IEEE/ACM TRANSACTIONS ON NETWORKING during 1992–2003. He received an NRC PIER Fellowship.